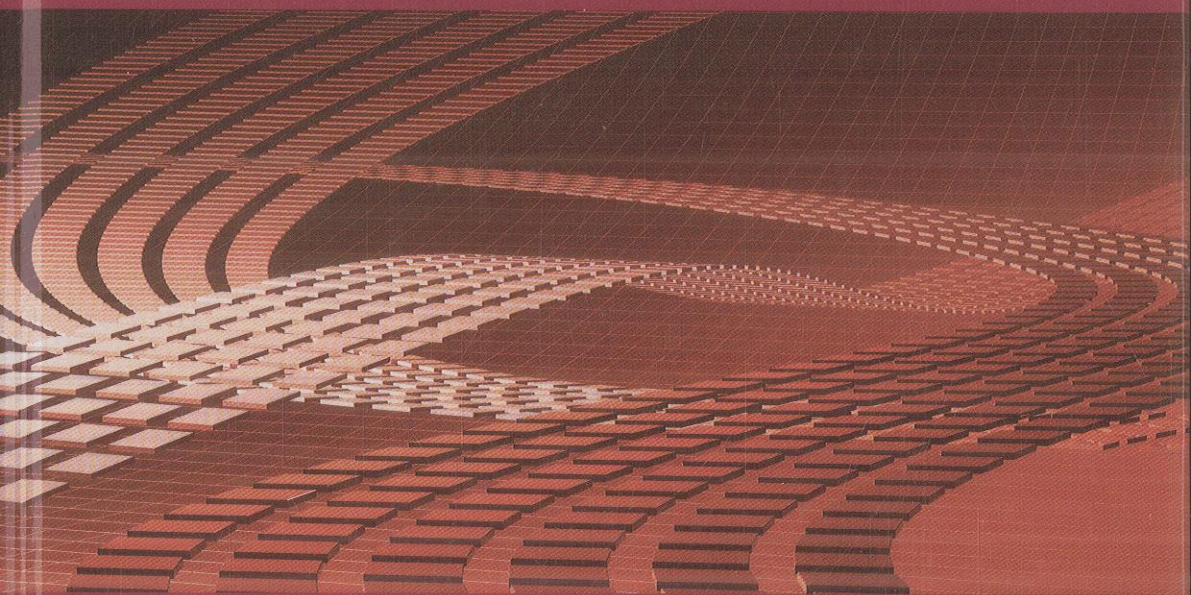


Mechanical Vibration and Shock Analysis



Specification Development

Volume 5

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ISTE

 **WILEY**

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